



# American Society of Naval Engineers (ASNE)

## Electrical Machine Technical Symposium (EMTS)

### *Integrated Systems Approach to Induction Motor Selection and Design*

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#### **Abstract**

Rotating machines have been critical to the technological advancements in manufacturing, shipping, energy, weapons systems, and everyday appliances. Over the past several decades, developments in electro-magnetic materials, power silicon devices, and especially computing power have enabled precipitous developments in power management and delivery. For example, ship propulsion used to be the exclusive domain of diesel engines or steam turbines – in recent years, however, practical implementations of electric motor propulsion have been employed with great success largely due to Variable Frequency Drive (VFD) technology and the associated digital controls.

In contrast to these developments, induction motors have changed very little since their invention by Nikola Tesla et al. in 1887<sup>1</sup>. Over the past century, there have been marginal improvements in materials, design techniques, and our fundamental understanding of the principles of operation but which have enabled nearly an order of magnitude increase in the power density of a typical industrial sized induction motor. Even with these advancements, induction motors have been leveraged predominantly in fixed speed applications – the relatively low cost and availability of VFD's in recent years has enabled broader use of the induction motor in many more applications than possible during the majority of the 20<sup>th</sup> century.

As with any technology, incremental developments are slow to be accepted or implemented for a variety of reasons:

- Entrenched use of the incumbent technology due to familiarity, confidence, and proven field service.
- Inter-component dependencies; constant speed pumps need constant speed motors.
- Perception of higher complexity when in many cases, systems can be made more efficient and simpler.

With the appropriate mindset, a skilled system designer will leverage all available technologies and design a system that will operate as efficiently and economically as possible over the desired operating envelope. It is the intent of this article to present one method to approach such a problem by utilizing computer simulation technologies.

#### **Technical Background Discussion**

##### *Introduction into Induction Motor Theory*

There are two common types of plots or graphs that describe the operation of an induction motor - constant frequency and variable frequency. The derivation of constant frequency graphs will be presented first since the variable frequency method is an applied extension of the constant frequency algorithm.

##### *Equivalent Circuit Model*

A fundamental construct used by scientists and engineers to model and describe the operation of an induction motor is the equivalent circuit<sup>2</sup>. The equivalent circuit is valuable because it can accurately predict the complex electro-mechanical interactions and operation of an induction motor using a relatively simple electrical network of linear components<sup>3</sup>. Figure 1 shows a representative example of an equivalent circuit model.

The component designations represent the following:

- $R_s$  = Stator Resistance at Nominal Temperature
- $X_s$  = Stator Leakage Reactance at the Design Frequency and Loading
- $R_r$  = Rotor Resistance at Nominal Temperature and Rated Slip

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<sup>1</sup> Scientific interest and development activity with regard to electric motors in this time period was intense. Records indicate that Nikola Tesla and Galileo Ferraris both independently developed a functioning induction motor...publishing their results within a month of each other. Further developments by intellectual giants at both GE and Westinghouse advanced the design of the induction motor over the next 8 years into the 'squirrel cage' design that is still used to this day.

<sup>2</sup> See Ref. A, B, C, D, and E

<sup>3</sup> Resistors and Inductors are all that is required. For the highest level of accuracy, non-linear components are required (resistors that are functions of frequency and temperature; inductors that are a function of current and frequency). Modeling of non-linear components requires copious amounts of empirical data and advanced numerical techniques beyond the scope of this paper.

- $X_r$  = Rotor Leakage Reactance at the Design Frequency
- $X_m$  = Magnetizing Reactance at the Design Frequency and Rated Excitation
- $R_c$  = Core Loss Resistance at Rated Excitation and Frequency
- $R_r'$  = Slip Derived Load Resistance;  $R_r' = R_r \cdot (1-s)/s$
- $s$  = Rotor Slip as a Ratio of Synchronous Speed;  $\{ s = 1 - N_r/N_s = 1 - (RPM \cdot poles) / (120 \cdot frequency) \}$

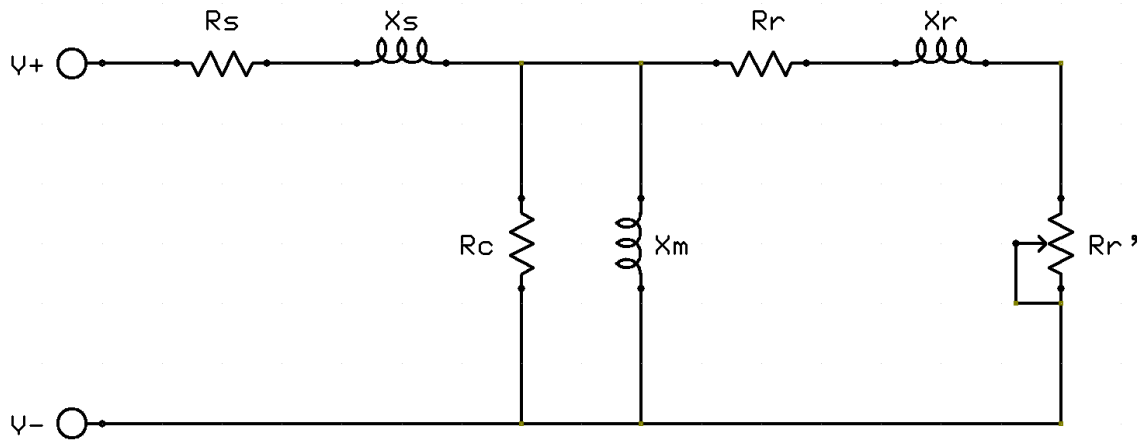


Figure 1 - Typical Equivalent Circuit Schematic Model of an Induction Motor

$R_s$ ,  $X_s$ ,  $R_r$ ,  $X_r$ ,  $R_c$ , and  $X_m$  are occasionally identified by different designations such as  $R_1$ ,  $X_1$ ,  $R_2$ ,  $X_2$ ,  $R_{fe}$ ,  $X_m$  or similar; the meaning of the components doesn't change and *usually*, it is pretty straightforward to understand the different designations or terminology. For the purposes of this paper,  $R_s$ ,  $X_s$ ,  $R_r$ ,  $R_c$ , and  $X_m$  will be used. It is important to keep in mind that the equivalent circuit model is really only modeling a single phase of an induction machine; any voltages and currents are phase referenced and any power or energy terms are multiplied by 3 to arrive at the output for the whole machine.

When the motor is operating under no-load, then the rotor speed is very nearly equal to the synchronous speed, therefore, slip is nearly equal to zero<sup>4</sup>. As slip approaches zero, the rotor branch resistance approaches infinity resulting in nearly zero current flowing in the rotor branch of the equivalent circuit – this allows the rotor branch to be approximated as an open circuit. With the rotor branch removed (no-load, open circuit), the circuit simplifies to that shown in Figure 2.

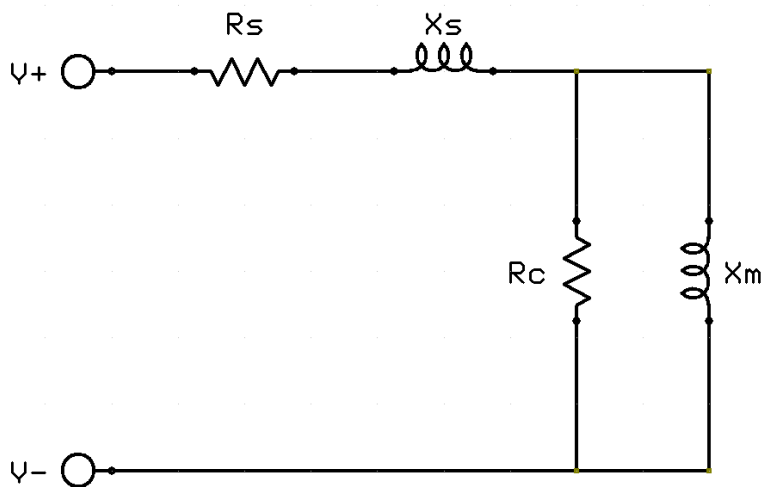


Figure 2 - No-Load Equivalent Circuit

<sup>4</sup> In practical motors, the no-load slip is on the order of  $10^{-3}$  to  $10^{-6}$

With the no-load circuit shown, the analysis simplifies to a simple network of the form:

$$I_s = \frac{V_s}{Z_t}; \text{ where } Z_t \text{ is the total no-load circuit impedance}$$

$$Z_t = Z_{R_s} + Z_{X_s} + (Z_m || Z_{R_c}) = R_s + jX_s + \frac{jX_m R_c}{R_c + jX_m}$$

$$Z_t = \frac{(R_s + jX_s)(R_c + jX_m) + jX_m R_c}{R_c + jX_m} = \frac{(R_s R_c - X_s X_m) + j(X_s R_c + R_s X_m)}{R_c + jX_m}$$

$$I_s = \frac{V_s}{Z_t} = \frac{V_s (R_c + jX_m)}{(R_s R_c - X_s X_m) + j(X_s R_c + R_s X_m)}$$

### Equation 1 - Calculation of No-Load Current

For no-load operation, near zero slip was assumed ( $s \cong 0$ ) which made the rotor branch impedance nearly infinite ( $R_r/s \cong \infty$ ) which allowed a simplification of the network into a more simple analytical network. Using similar techniques, we can mechanically constrain the shaft with electrical power applied, making the slip equal to 100% ( $s = 1$ ). In practical induction motors, the value of  $X_m$  is much greater than the entire impedance of the rotor branch with the rotor locked (very small impact on circuit impedance); applying this simplification, we arrive at the following simplified circuit (Figure 3):

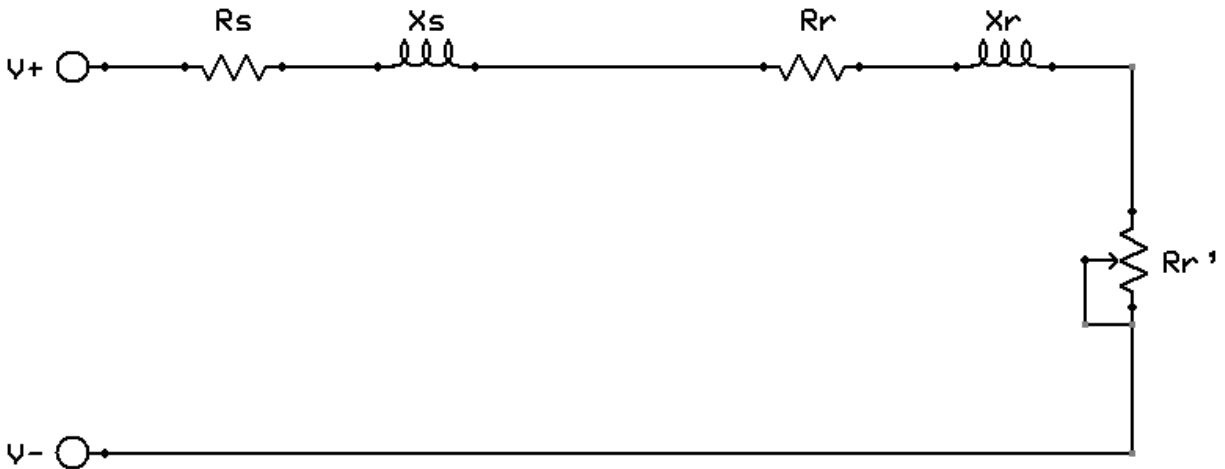


Figure 3 - Locked Rotor Equivalent Circuit

In this condition, the stator current equation simplifies to the following:

$$I_s = \frac{V_s}{Z_t}; \text{ where } Z_t \text{ is the total locked rotor circuit impedance}$$

$$Z_t = Z_{R_s} + Z_{X_s} + Z_{R_r} + Z_{X_r} + Z_{R_{r'}}$$

$$Z_t = R_s + X_s + R_r + X_r + R_{r'} \left( \frac{1-s}{s} \right) = R_s + X_s + R_r + X_r$$

$$I_s = \frac{V_s}{Z_t} = \frac{V_s}{R_s + X_s + R_r + X_r}$$

### Equation 2 – Calculation of Locked Rotor Current

The two simplified methods described above are important in the analysis of induction motors because it is relatively simple to conduct no-load and locked rotor tests and measurements on induction motors. From these measurements, reasonably accurate values of the equivalent circuit parameters can be obtained if the manufacturer's data is not available or is in question.

Thus far, we have studied an induction machine equivalent circuit with  $s=0$  and with  $s=1$ ; for any other operating point, the circuit analysis gets slightly more difficult. The standard Steinmetz equivalent circuit outlined in Figure 1 must be solved for all values of slip ( $0 \leq s \leq 1$ ) over the entire operating range of the motor under study. Modern day computing makes calculating and tabulating these values at thousands of operating points quick using numerical techniques, however, a simplified analytical method is frequently used by employing the Thevenin equivalent of the circuit. This method effectively combines, as shown in Figure 4, the portions of the circuit that remain constant ( $X_m$ ,  $R_s$ ,  $X_s$ , &  $R_c$ ) into a single voltage supply, lumped inductance, and lumped resistance. In this form, an analytical analysis is straightforward and takes the final form:

$$I_s = \frac{V_{th}}{Z_{th}} = \frac{V_{th}}{R_{th} + X_{th} + R_r + X_r + R_r \frac{(1-s)}{s}} = \frac{V_{th}}{R_{th} + X_{th} + X_r + \frac{R_r}{s}}$$

Equation 3 - Stator Current for Equivalent Circuit; Nominal Operation

In this simplified form, the circuit effectively becomes a simple series linear reactive circuit with a single variable (the motor slip). As slip is varied, thermal losses and shaft power delivered can be easily calculated as follows:

Per Phase Stator Thermal Output

$$\dot{Q}_s = I_s^2 R_s$$

Per Phase Rotor Thermal Output

$$\dot{Q}_r = I_r^2 R_r$$

Per Phase Mechanical Power Output

$$P_{mech} = I_r^2 \frac{R_r}{s}$$

Speed

$$RPM = 60 * \frac{\omega_r}{2\pi} = \omega_s(1-s)$$

Per Phase Torque

$$\frac{P_{mech}}{\omega_r} = \tau = \frac{P_{mech}}{\omega_s(1-s)}$$

Per Phase Electrical Power Input (Apparent, Reactive, Active)

$$S_{elex} = V_s I_s; \quad Q_{elex} = \sqrt{S_{elex}^2 - P_{elex}^2}; \quad P_{elex} = V_s I_s * pf$$

Efficiency

$$\eta = \frac{P_{mech}}{P_{elex}}$$

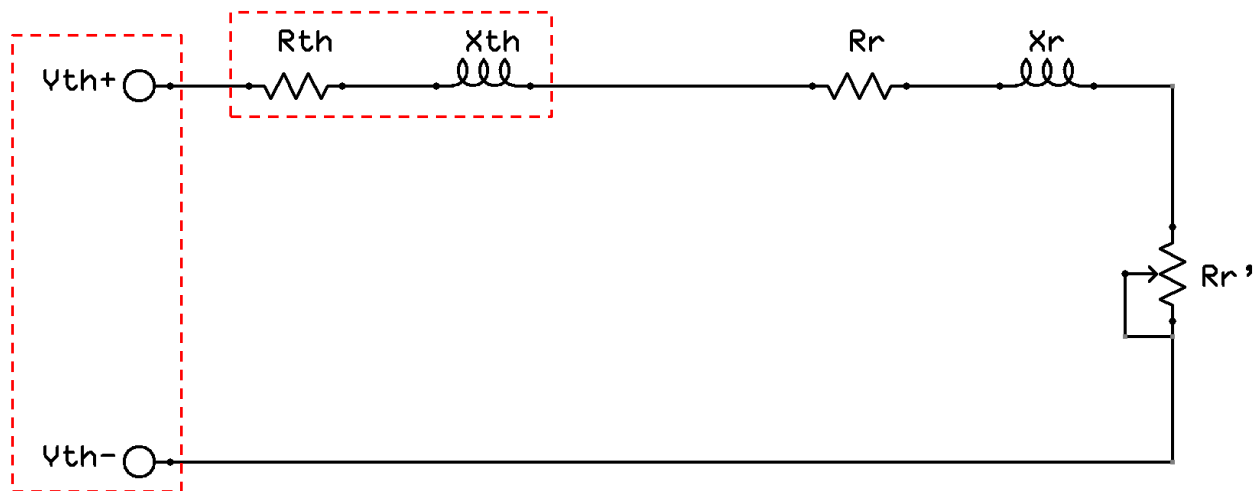


Figure 4 - Thevenin Equivalent Circuit Model

Beware that the above equations represent the parameters for only one of the three phases...for a balanced three phase machine; the above values must be converted appropriately:

- Voltages and currents are corrected based on the motor connection (delta or wye)
- Powers and torques are multiplied by three
- Other intrinsic properties are left unchanged (RPM, slip, efficiency, etc).

### Application of the Equivalent Circuit Model – Fixed Frequency Operation

For constant temperature, load, voltage, and frequency, a set of 'Fixed Frequency Performance Plots' can be generated that plot parameters against slip (...or more commonly, shaft speed). An example of a torque curve and current curve are shown in Figure 5 and Figure 6:

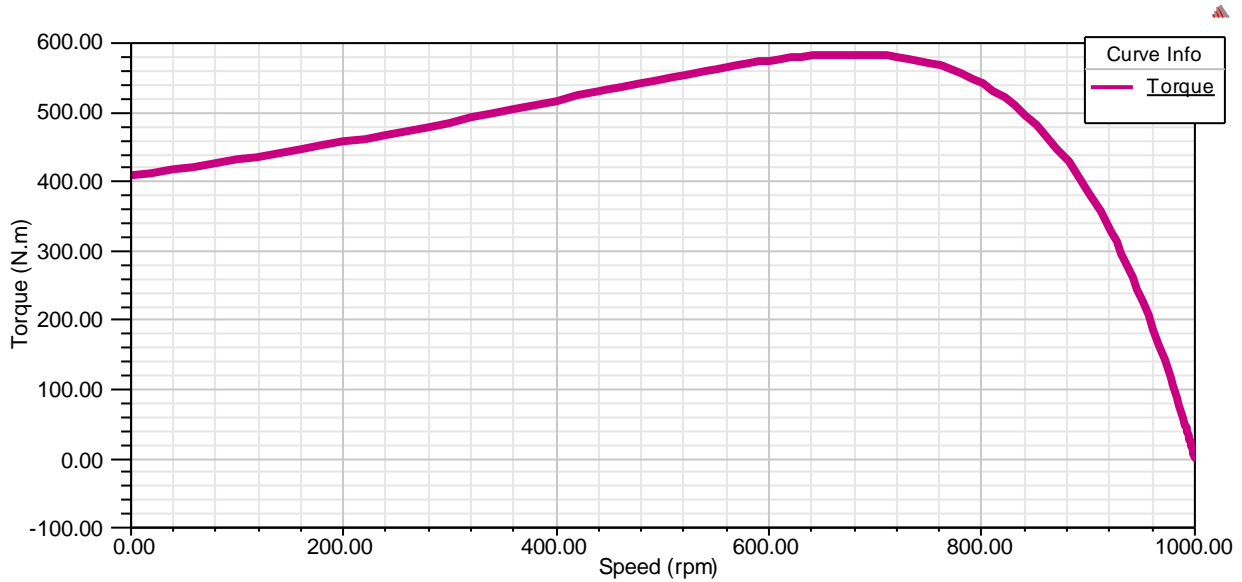


Figure 5 - Fixed Frequency; Torque vs. Speed

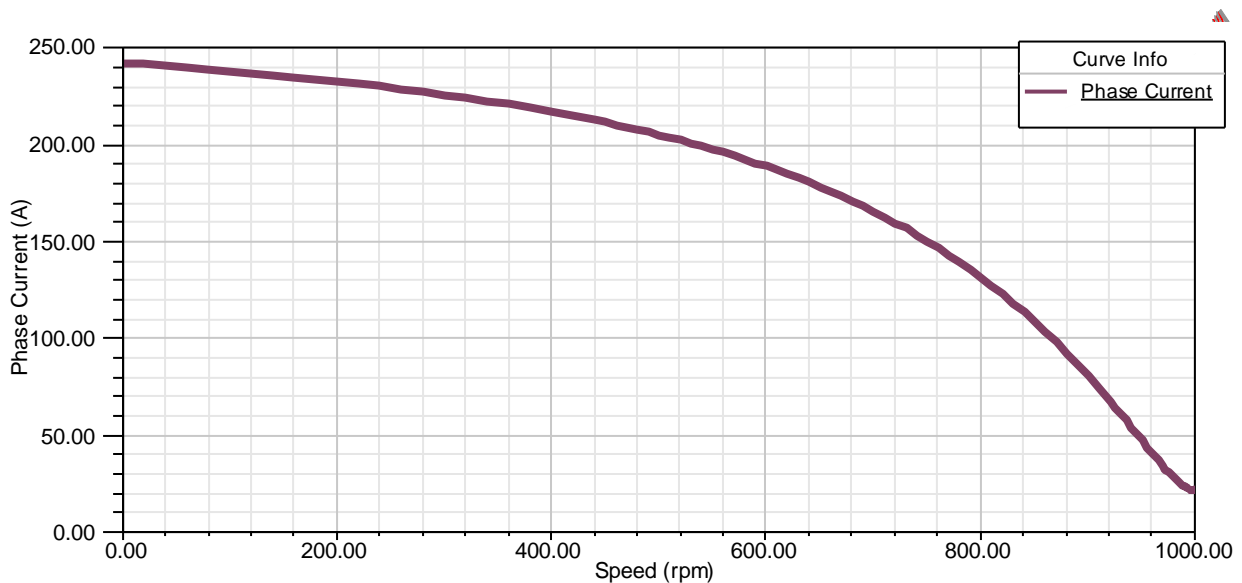


Figure 6 - Fixed Frequency; Phase Current vs. Speed

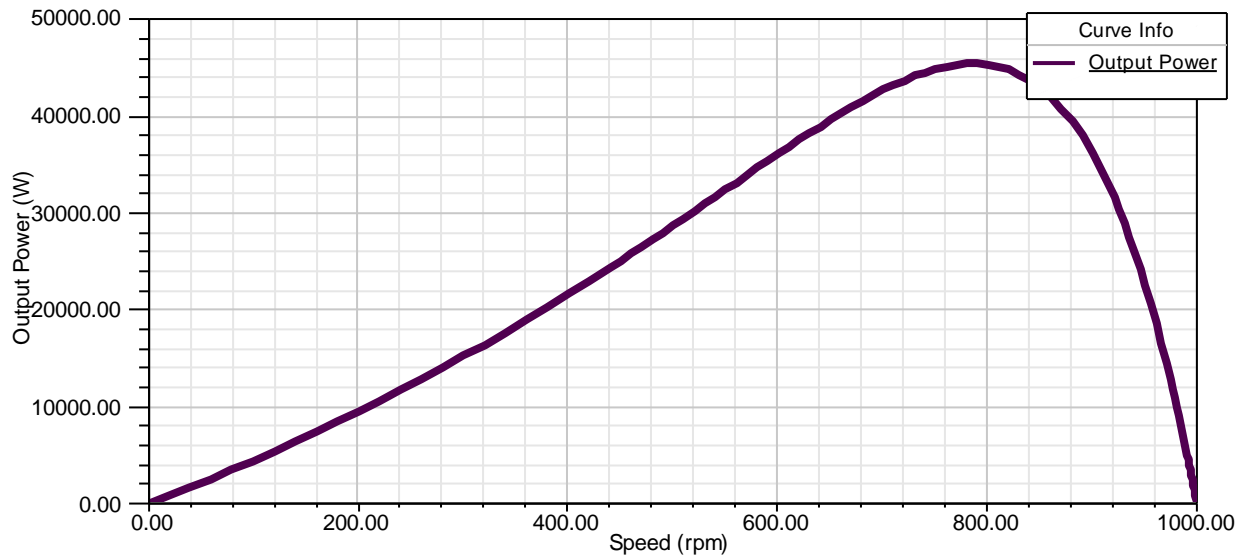


Figure 7 - Fixed Frequency; Output Power vs. Speed

A collection of curves can be derived for virtually any combination of parameters using the provided equations (effects of varying frequency, voltage, or coil temperature can be qualitatively evaluated quickly).

*Application of the Equivalent Circuit Model – Variable Frequency Operation*

By applying the Fixed Frequency techniques and sweeping input frequency, we can create a family of curves (or a surface) that represents motor performance over a range of input frequencies and slip simultaneously. Since synchronous speed is determined by motor construction and input frequency, we can control motor speed in a given motor by varying the input frequency (...similarly, varying the armature voltage will vary the speed in a brushed DC motor). Variable frequency drives are designed precisely for the purpose of controlling the frequency of the voltage delivered to an induction motor, compensating for intrinsic slip, to control the motor shaft speed at least as good or often better than can be achieved with a DC motor.

An induction motor is inherently inductive – the impedance to current flow varies with the input frequency. Ideal inductor impedance is calculated by:

$$Z_L = j\omega L = j2\pi fL \quad ^5$$

One will quickly notice by inspection that impedance and frequency are directly proportional; as frequency increases, inductive impedance increases at the same rate. In order to maintain a constant RMS current into an inductor as frequency is increased, the input voltage must increase by the same proportion as the frequency. In variable frequency applications, this is commonly referred to as the “Volts per Hertz Curve” or just “V/f”. For frequencies below the design frequency and voltage, the V/f curve takes the following shape:

<sup>5</sup> Here, ‘j’ represents the phasor operator such that the resultant current in a purely inductive circuit is exactly 90° out-of-phase with the excitation source.

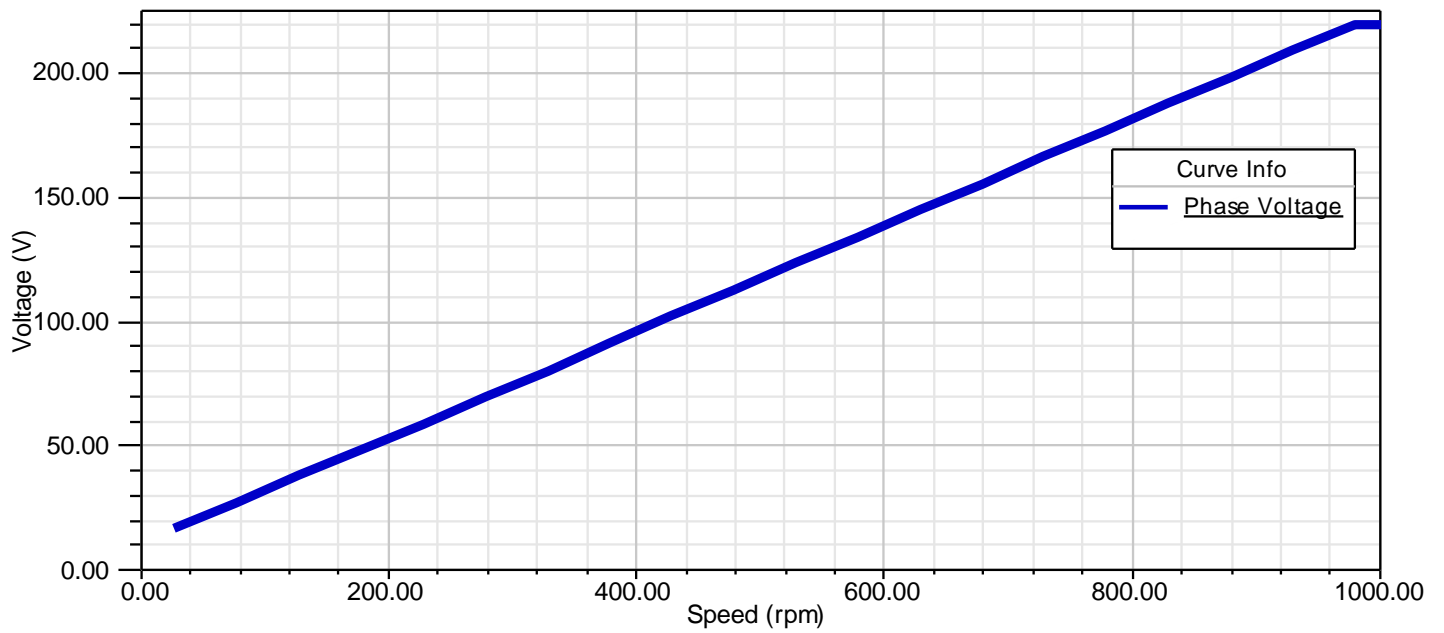


Figure 8 - Phase Voltage vs. Speed for Variable Frequency Operation

If we were to apply this technique, sweeping frequency while constraining input voltage to follow the V/f curve, we produce the following family of curves:

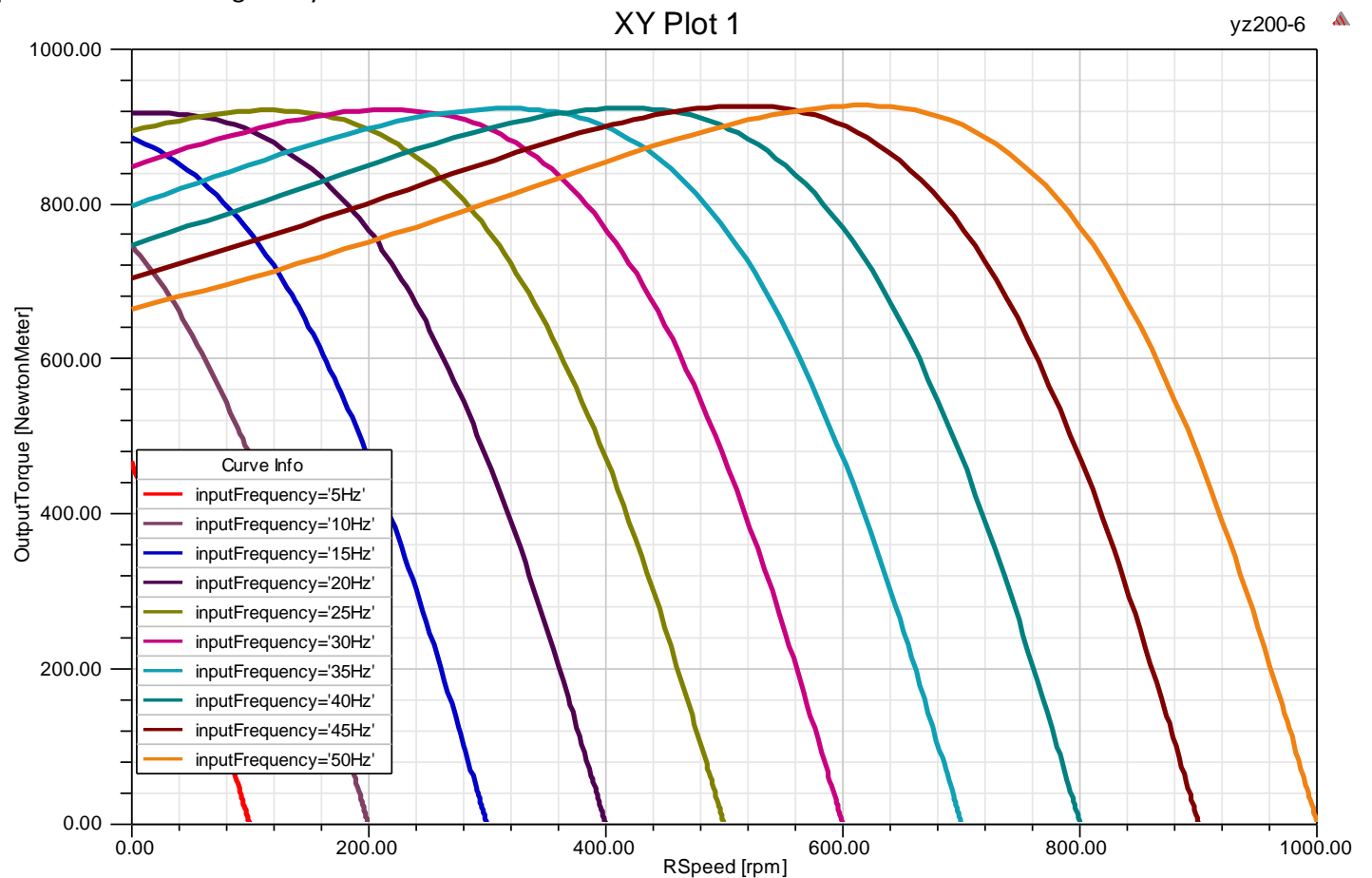


Figure 9 - Torque vs. Speed Curve at Several Fixed Frequencies

By matching the applied voltage and frequency to the electrical properties of the motor, control of the motor is simplified and produces an approximately constant torque capability between low speed and nominal speed. As a



consequence of the mechanical power equation, the shaft RPM and shaft mechanical power are directly proportional to each other (the proportionality constant being the constant torque rating):

$$P_{mech} = \omega \vec{\tau}$$

### Motor Performance Curves; Zero Speed to Nominal Speed Variable Frequency Operation

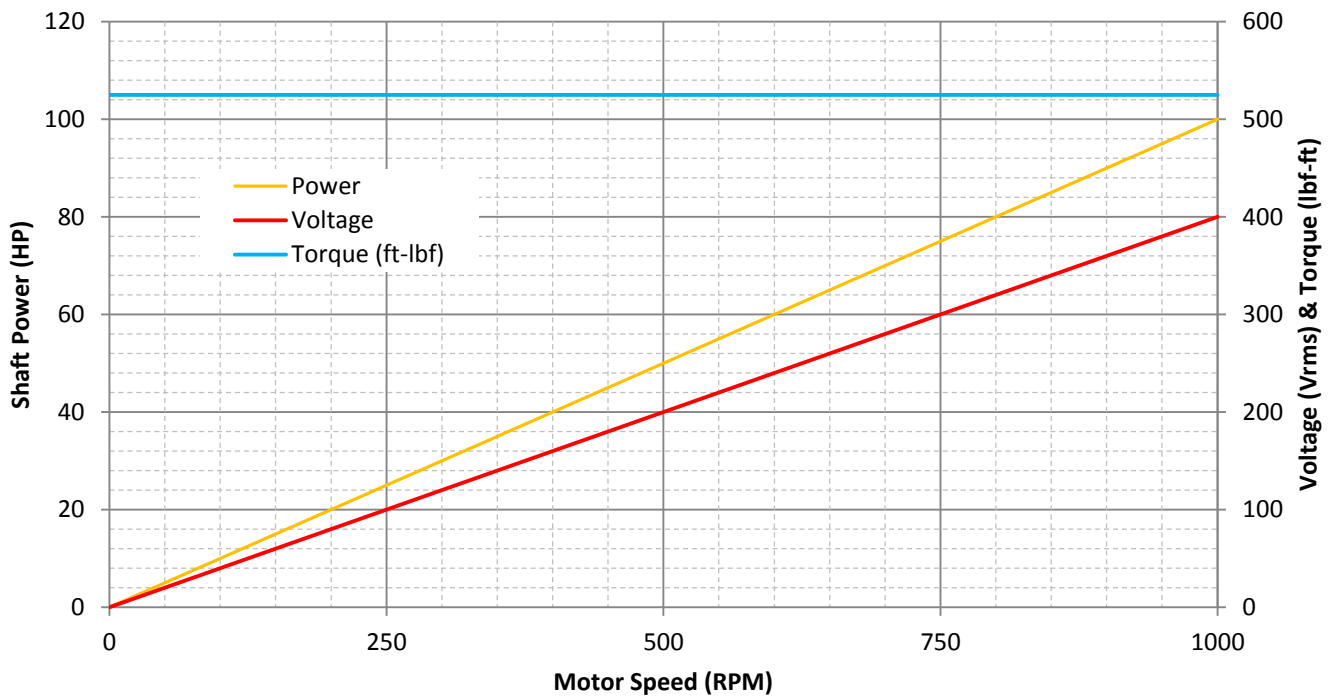


Figure 10 - Motor Power, Voltage, and Torque vs. Speed; Variable Frequency Operation - Constant Torque Region

This type of control in a VFD is termed 'Scalar Control'; most industrial VFD's will include Scalar Control as well as much more advanced control algorithms that incorporate electrical and mechanical motor feedback to enhance dynamic properties, efficiency, and low speed performance<sup>6</sup>.

Theoretically, voltage and frequency could be increased in accordance with the V/f constant without limit (maintaining a constant torque all the way to maximum speed); however, practical considerations place constraints on this. The VFD will have a maximum input & output voltage limit based on maximum component voltage withstand ratings.

Additionally, the insulation materials within the motor place constraints on the maximum terminal voltage that may be applied to the motor. The net result is an increasing voltage from the VFD as output frequency increases - retaining compliance with the V/f curve until the drive output voltage reaches any of the following:

- The amplitude of the output voltage is near the input power supply peak voltage to the VFD (for simple input rectification schemes).<sup>7</sup>
- The VFD output voltage reaches the motor rated voltage programmed into the drive (nameplate base voltage).

If the drive output frequency continues to increase above the nameplate base/rated frequency without a corresponding increase in output voltage, the motor is said to be operating in the 'Flux Weakening Mode'. As a consequence of the inductive effects relating frequency and impedance, the maximum torque that can be generated falls off as frequency continues to increase (constant voltage, increasing frequency  $\Rightarrow$  impedance increases, current decreases, field intensity decreases). This effect limits the maximum power capability of the motor at higher speeds due to thermal limits (discussed later in this paper) and due to proximity to the stall torque of the motor. While operating in Flux Weakening Mode, the maximum power the motor is capable of is approximately constant, hence this region being termed the

<sup>6</sup> Advanced control algorithms and output stage structure within a VFD are beyond the scope of this paper; for further reading, common search terms include : Direct Torque Control, Vector Control, Torque Control, and Sensorless Vector Control

<sup>7</sup> Some VFD designs incorporate a voltage boost circuit to enable higher output voltages than are provided by the input power supply. A drive with this capability could be used, for example, to power a 440V motor from a 400V 50Hz supply.

'Constant Power Region'. Because the  $P_{mech}$  limit remains approximately constant as frequency/speed is increased, the rated torque tends to decrease following an inverse law (  $speed^{-1}$  or  $frequency^{-1}$ ):

$$\tau = \frac{\overrightarrow{P_{mech}}}{\omega}$$

The initial performance curve of Figure 10 can now be expanded to include the Constant Power Region / Flux Weakening Mode as shown here:

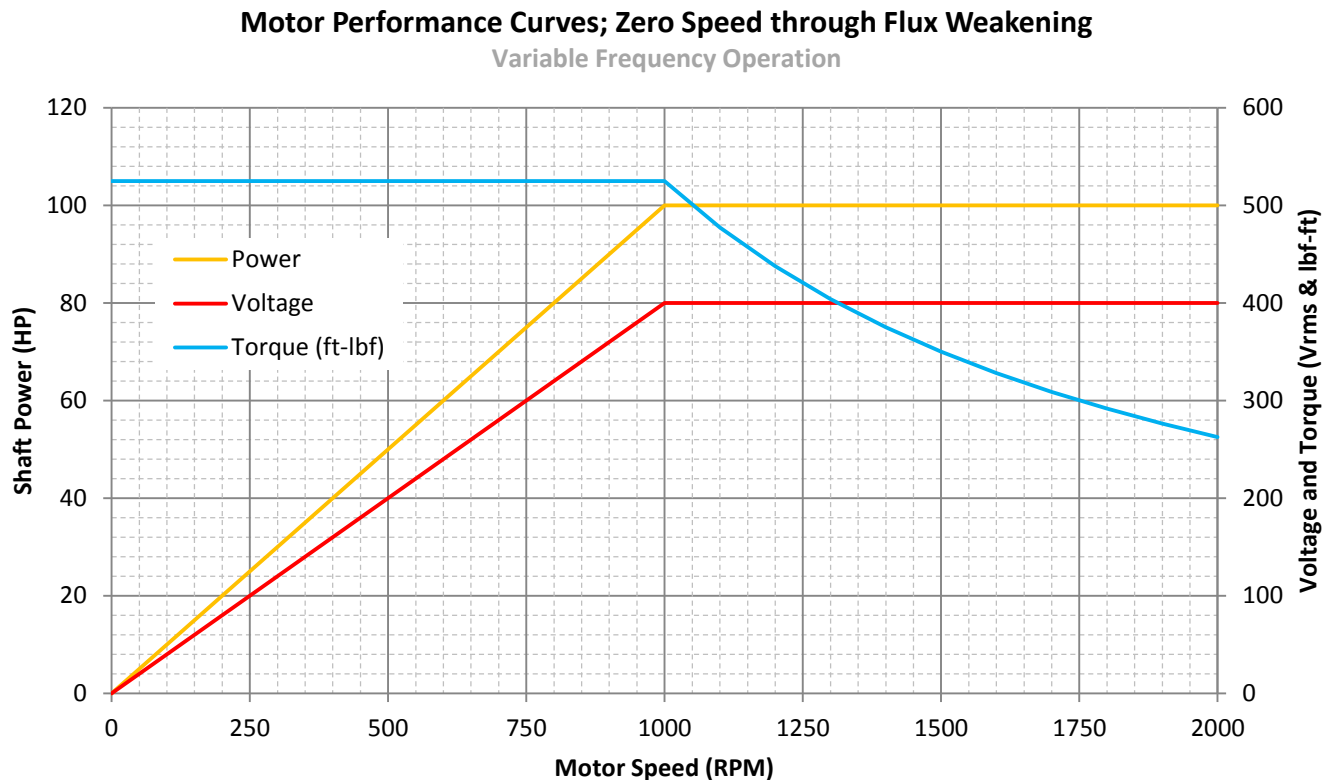


Figure 11 - Induction Motor Performance Curve

Adopting the simplified performance curve as shown in Figure 11 ensures that thermal limits are not exceeded and enables implementation of relatively simple adaptation algorithms.

Up to this point, all analysis has been performed by utilizing first principles equations and a simplified equivalent circuit model with constant coefficients; detailed analysis for the purposes of optimization or use in a particular application require incorporation of non-linear effects, transient analysis, and the contribution of driven system physics.

## Motor Centric System Analysis

Optimizing motor construction and design for a particular application requires much more in-depth analysis and well defined operating criteria so that effective trade-offs may be made at design time. To this end, we must resort back to numerical/recursive techniques in order to model motor behavior for transient conditions and compensate for non-linear material effects by incorporating detailed solid modelling, 2D and 3D Electromagnetic FEA, 3D Computational Fluid Dynamics, and customized numerical analysis models for the coupled system.

### *Identifying Design Goals and Constraints*

Smaller induction motors have differing design challenges than do larger motors but nearly all motor sizes must adhere to a fixed set of design goals and constraints for the application:

- Base Output Power
- Operating Voltage
- Required speeds and torque profile
- Efficiency constraints
- Drive Method (across-the-line, soft start, wye-delta start, or variable frequency drive)
- Size and Weight
- Constraining dimensions (length, diameter, etc)
- Power source characteristics (maximum current, voltage supply 'stiffness', harmonic content, etc)
- Structure borne or Acoustic noise limits
- Operating life and maintenance
- Reparability
- Environmental requirements
- Mounting orientation/interface methods
- Transient performance requirements
- ...and of course, cost

For some applications, low speed or breakaway torque is immaterial but absorbing load transients at higher speeds *is* critical. Another application may be heavily focused on size and weight. Most sub-surface military applications focus on efficiency and noise reduction. Yet other applications would rely on a low initial purchase price with little regard to lifetime operating costs. In each of these cases, otherwise identical electrical and mechanical specifications would result in vastly different optimized motors for each of these applications - too often, systems designers select motors based on a limited understanding of how that selection may affect overall system performance and efficiency or may tend to focus too heavily on motor construction details that have little impact on the intended application. By understanding which specifications affect motor design and performance, the system designer can more effectively communicate needs and discuss trade-offs, perhaps even incorporating mechanical system and electrical system design choices to arrive at an optimum motor selection from the perspective of the overall integrated system.

For the purposes of this example, we will select a set of fictitious requirements and attempt to optimize a design to accommodate these requirements. During this process, we will also be able to identify areas for potential improvements to the system based on the resulting capabilities of the motor as the design progresses.

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## Application

- Surface Marine Propulsion
- Twin screws
- Fully redundant

## Power Rating

- 20,000 HP total (flank)
- 5,000 HP minimum (single failure)

## Electrical Specifications

- Variable Frequency Drives; two-level outputs
- 4kV max voltage

## Mechanical Specifications

- Maximum volumetric envelope of 8' x 6' x 6' for each motor
- Weight allowance of 30,000 lbs per drive motor (~8 lbs / kW)

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## Implied Constraints

- Average Density = 104 lb / ft<sup>3</sup>; (solid steel is ~553 lb / ft<sup>3</sup>)
- Reliability is important
- Field serviceable (not easy to replace)
- Each motor is 5000HP
- Stall torque/break-away torque not critical (a ship's propeller approximates the pump laws where  $P \approx k \cdot N^3$ )
- Bi-directional operation required
- Transient performance important (emergency back full)

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## Missing Constraints / Free Variables

- Cost of electric power (gas-turbine or diesel; aggregate \$/kW of electric power)
- Current Capacity of Drive and Upstream Electric Equipment
- Typical Operating Profile
- Method of waste heat rejection (air cooled, water cooled)
- Desired motor speed range (screw speed with or without gearbox)
- Overload requirements
- New design ship or retro-fit/replacement?

During preliminary design, implied or assumed design goals and any missing information would be settled by interview and several discussions focusing on the technical goals; for the purposes of this example, these details will be ignored.

On some occasions, the screw design and drive train details will have been long settled before detailed drive motor specifications are begun; for this example, we will assume that the remainder of the propulsion system can still be negotiated.

### Detailed System Analysis

Any motor design optimization effort must begin with an understanding of the driven load. From a first principles perspective, the designer should consider how the load profile will affect design; for a ship's screw, shaft, and other transmission components, we can approximate this behavior by considering the following polynomial model:

$$P_{shaft} = K_1 \omega_{shaft} + K_2 \omega_{shaft}^2 + K_3 \omega_{shaft}^3$$
$$\tau_{shaft} = K_1 + K_2 \omega_{shaft} + K_3 \omega_{shaft}^2$$

Where:

$P_{shaft}$  is the power delivered by the motor in Watts

$\omega_{shaft}$  is the angular velocity of the shaft in sec<sup>-1</sup>

$K_1$  accounts for the constant torque components in the drivetrain (in N-m)

$K_2$  accounts for the torque components that are dependent on drivetrain speed (in N-m-s)

$K_3$  accounts for the torque needed to rotate the screw; (in N-m-s<sup>2</sup>)

By applying these principles, the following characteristic plots are generated:

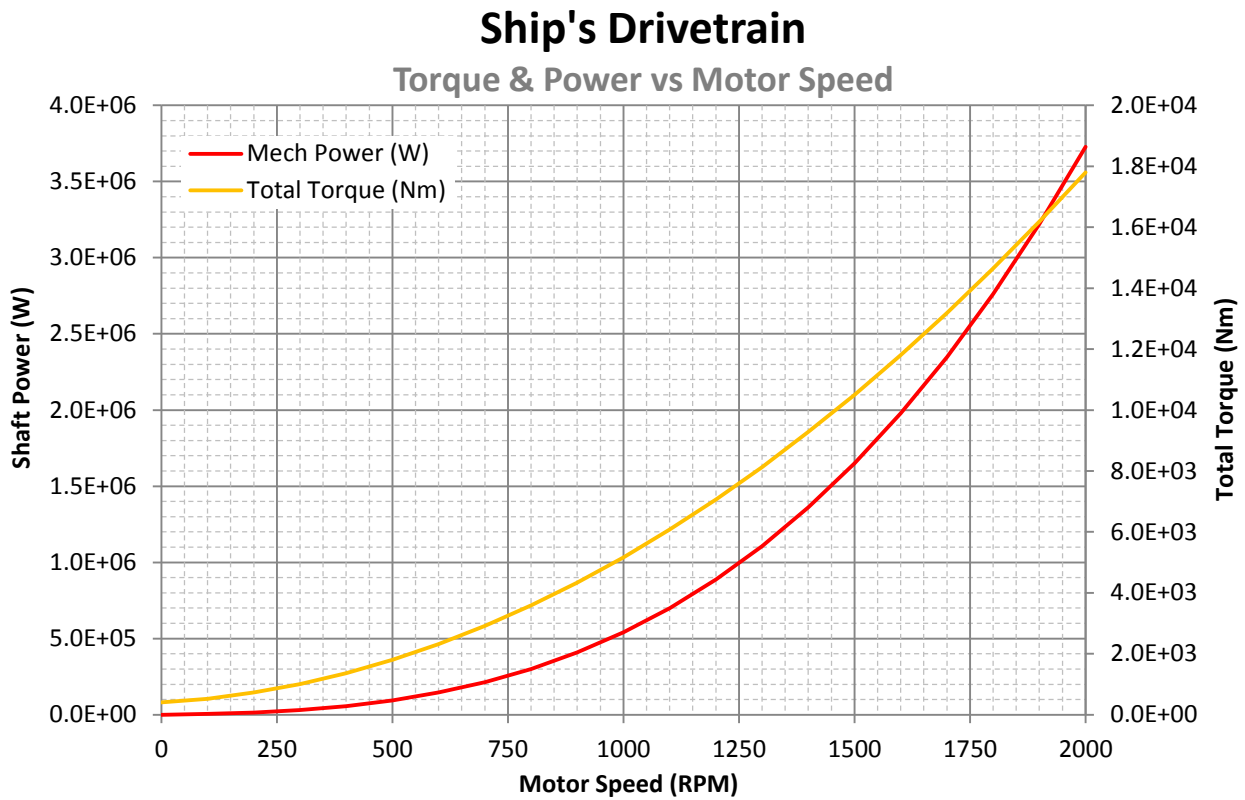


Figure 12 – Simple Numerical Model of Motor Torque and Power;  $K_1=406$ ,  $K_2=7.87$ ,  $K_3=0.359$

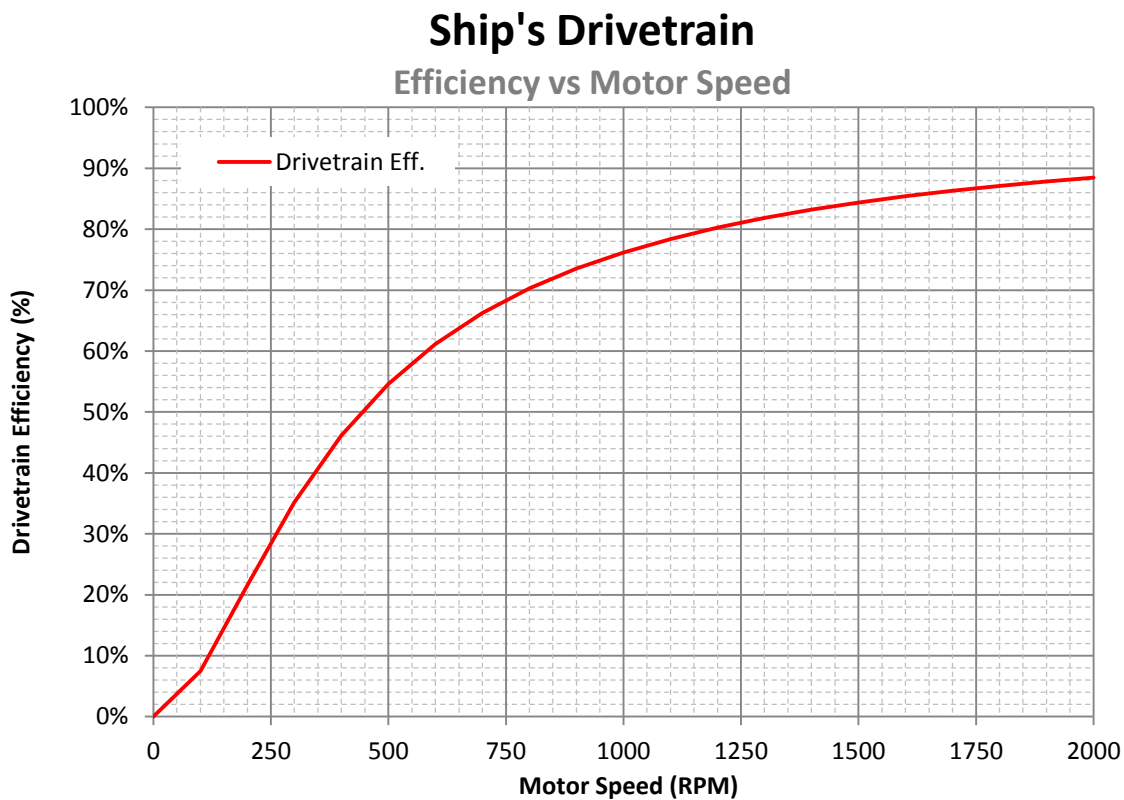


Figure 13 - Simple Numerical Model Drivetrain Efficiency

By inspection we notice some key characteristics of this system that will heavily influence motor design:

- The torque required of the motor at low motor speeds is quite low but increases with speed at an accelerating rate (typical of a fluid pump application)

- The motor will not be able to achieve full torque until the drivetrain is at full speed
- The maximum efficiency of the drivetrain is approximately 88%; rejecting about 430kW as heat.
- Ship's Shaft Horsepower (SHP) is 4423 HP

With a suitable drivetrain model, the other efficiencies in the system can be considered. A typical medium voltage drive at this power level is expected to be ~97% efficient while a typical induction motor should be ~95% efficient at full power resulting in an electric power requirement of 3.92 MW into the motor and 4.05 MW into the drive; drive heat generation is ~126 kW and motor thermal losses amount to about 192kW. The drivetrain clearly represents the bulk of the thermal losses in this case; investment in improved drivetrain design to increase efficiency could provide benefit but only to a point...after which drivetrain capital expense would exceed budgetary constraints. With an assumed motor power factor of ~0.85, the drive current rating needs to be at least 665A @ 4kV.

For the sake of this example, we will assume that the drivetrain utilized a two-stage gear reduction to match the motor max speed of 2000 RPM to the flank screw speed of perhaps 200 RPM. A plausible approach might be to consider matching as closely as possible the full power motor speed to the full power shaft speed such that the gear reduction along with the associated losses could be eliminated. An additional consideration should also be the removal of ancillary gear train lubrication and cooling capacity as well as reduced maintenance requirements. The synchronous speed of an induction motor can be calculated using the following relation:

$$N_{synch} = \frac{120 * f}{N_{poles}}$$

Given that the system already incorporates a variable frequency drive, we are liberated in selecting any convenient electrical frequency necessary (within the capability of the VFD) in order to achieve the required synchronous speed. The variable of interest in this case is the number of motor poles,  $N_{poles}$ . The number of motor poles is constrained to be an even number (minimum of 2) but could theoretically increase without limit allowing the motor designer to achieve a very low synchronous speed.<sup>8</sup> Unfortunately, very few engineering problems allow for gain without some compromise...in this case, motors with a higher number of poles generally suffer from reduced efficiency, increased size, and degraded power factor (higher reactive current flow).

Any reductions in motor efficiency are likely to be swamped by the gains in drivetrain efficiency.<sup>9</sup> The degradation in power factor will have a meaningful impact on drive selection and perhaps upstream electrical distribution system components. For example, a 24-pole motor of this size and rating may have a design power factor as poor as 0.65 resulting in motor currents as high as 830A. The drive silicon component size would increase by approximately 25% and resultant drive losses would increase as well. While the motor power factor is poor, drive technologies exist which provide power factor correction at the point of use and are designed in as an integral feature of the drive. Naturally, drive costs increase but are likely a fair trade-off compared to increasing the capacity of the electrical distribution system of the ship. Even when considering extra capital cost associated with larger, more sophisticated drives, the elimination of the gear reduction along with elimination of the lubricating system and associated costs would more than pay for the increase in drive costs.

Since the drivetrain will now be much more efficient (~98%), the client will have a decision to make:

- Increase the shaft horsepower rating since a larger proportion of the motor shaft power will be delivered to the screw (thereby increasing maximum ship's speed).
- Or, decrease the electric motor power requirement commensurate with the decrease in gear losses.

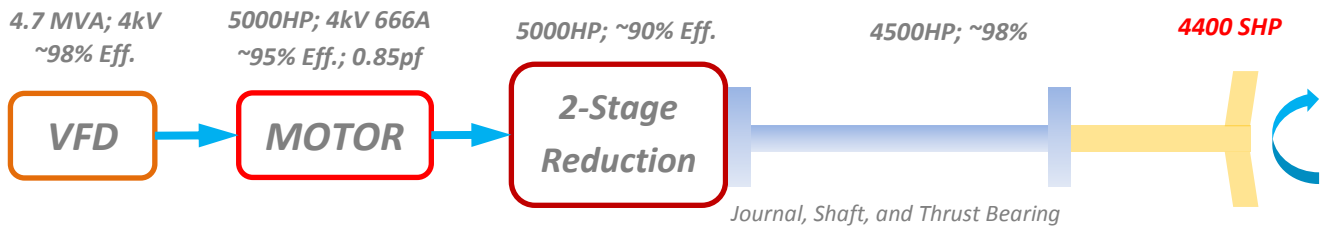
If we were to assume that this was not a performance critical application, then the client would likely opt for a smaller, lower power, less expensive motor. An extra advantage of opting for this path would be a reduction in VFD capacity necessary, perhaps back to that originally budgeted before excess capacity was required to accommodate the higher pole count.

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<sup>8</sup> For example, a nominal frequency of 40Hz applied to a 24-pole induction motor will result in a synchronous speed of 200 RPM. 20Hz applied to a 12-pole induction motor would also result in 200 RPM. By understanding this, the motor designer can achieve an optimized design by conducting trade-off analysis between drive, motor, and drivetrain to optimize on efficiency.

<sup>9</sup> By eliminating the two-stage gear reduction, the remaining mechanical losses downstream of the motor are journal bearing, thrust bearing, and other shaft losses...drivetrain efficiency may be as high as 98% in this case.

## Original Drivetrain Architecture



## Modified Drivetrain Architecture

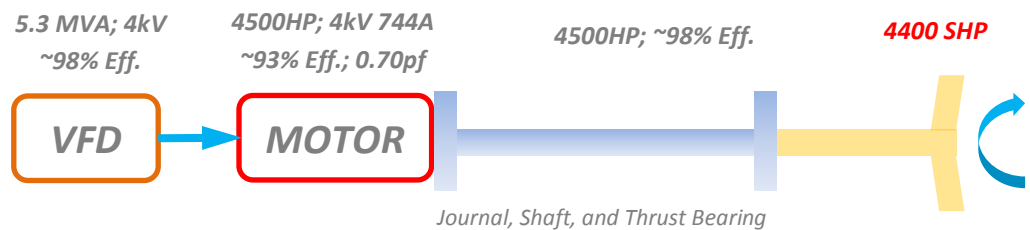


Figure 14 - Comparison of Competing Drivetrain System Designs

We quickly realize that the VFD ratings did in-deed increase from 4.7MVA to 5.3MVA (~12.7%) but the removal of the gear reduction provided extra space in the engine room, weight savings, reduction in overall system cost, reduced system inertia, and lower maintenance requirements.

### Detailed Motor Design and Analysis

With a revised propulsion motor specification, the motor designer can begin the task of detailed design and analysis. In most engineering disciplines, experience will often provide a good starting point for any design effort and this case is no different. The motor designer can begin with a rough approximation of the motor geometry based on experience and modify specific dimensions as the design progresses to achieve the desired specifications.

We will begin our design with the following:

- 48" Stator OD (1200mm)
- 36" Stator Length (1000mm)
- Examine both 12-pole and 24-pole solutions
- Must be form-wound (rectangular stator slot profile)
- 4000V
- 4500HP
- 93% minimum efficiency
- 0.70 minimum power factor

**Weight** - The estimated weight of the motor core (stator, windings, rotor, and connections) can be approximated by calculating the volume of the cylinder enclosed by the stator dimensions and calculating a weight based on the density of steel. While this is a crude method, it serves as a good indicator as to where further optimization effort should be placed. For this example, the estimated weight of the core is 20,835 lbs; this represents about 2/3 of our original weight limit of 30,000 lbs. This leaves a reasonable margin for frame, bearings, shaft, and other necessary components to safely operate the motor.

**Size** – The frame width should not be much larger than the stator OD of 48" (~1200mm). The length of the frame is dependent not only on the core length, but also on the length required for the stator end-turns, phase rings, and end-bell details. Generally, higher pole count motors will have a shorter end-turn length but larger stator diameter; higher coil pitch will result in end-turns that protrude further. We will assume for the time being that our end turn extensions are 10" which would make the frame approximately 78-82" long. It appears that we will be within the design goal of 6' x 6' x 8'.

**Performance** - Figure 12 & Figure 13 provide the load profile for a 5000 HP motor at 2000RPM (with the gear reduction in place).

**Torque** – The motor is required to deliver 4500HP at 200RPM which equates to 118,170 lbf-ft (160,217 N-m). Assuming a solid circular shaft, the following relation identifies the minimum shaft diameter to operate at the material limit:

$$D_{min} = \sqrt[3]{\left(\frac{16T_{max}}{\pi\tau_{max}}\right)}$$

For 4340 steel,  $\tau_{max}=7.10e+08$  Pa  $\Rightarrow D_{min}=105$ mm. Since this is a critical application, we will apply a margin of safety of 5, therefore, the design shaft diameter is 180mm.

At this stage, electrical machine design & numerical modelling tools<sup>10</sup> are utilized to begin some of the analysis. The machine design tools automatically perform most of the tedious calculations for the designer enabling a better focus on optimization and design choices.

#### *Selecting the number of rotor and stator slots*

Selection of slot count is a blend of art and science. There are general rules to be followed for slot numbers and slot ratios but most of these have to do with electrical harmonics, torque pulsations, or other minor inefficiencies. A few fundamental rules should however be followed:

- The number of stator slots and number of rotor slots should be significantly different (perhaps 120 & 91). It typically doesn't matter if the rotor has more or less slots so this detail is left to the designer
- The number of stator slots *must* be an even multiple of the product of phase-count and number of poles for symmetric wound stators. For our 24-pole machine, we may select 3x24=72, 144, 216, 288 ... as our number of stator slots.
  - o To start, the slot width multiplied by the number of slots should be about 40%-60% of the stator inner circumference.
  - o Motor winding, especially in large machines, remains a labor intensive process performed by skilled personnel. The stator slot should be wide enough to make inserting coils manageable but not so wide that the coils become unwieldy (a coil 60" long and 1" wide will not be flexible and will be quite heavy, risking damage to the insulation during insertion).

For this exercise, we will select 144 slots as this is an even multiple of both 12 and 24 (the two pole combinations under consideration) and will keep the slot width around 3/8". This will allow us to study the advantages of one pole combination over the other without impacting the stator or rotor geometry.

#### *Selecting the Stator ID & Rotor OD (as well as air gap)*

Electromagnetically, the ideal motor would have no air gap; however, this is not practical. Air gap distance is usually chosen based on safety margins related to rotor diameter, maximum speed, bearing tolerances, and manufacturing tolerances. In our example, 1mm should be adequate to ensure sufficient gap at these speeds.

Selecting a starting point for stator ID is a balance between sufficient back-iron and maximizing the stator ID for torque generation<sup>11</sup>. Additionally, higher pole count motors require less back-iron than their lower pole count equivalents. For this exercise, we will begin with a stator ID that is 75% of the stator OD (75% x 1200mm = 900mm).

#### *Selecting the Number of Coil Turns*

<sup>10</sup> In this case, Ansoft® RMxprt and Maxwell

<sup>11</sup> Generated torque will be proportional to the circumferential speed of the rotating magnetic field which will be higher for larger diameter stators thereby requiring less rotor slip to generate the necessary rotor currents. However, larger ID stators also require more coil-copper which may increase cost, weight, and thermal losses.



The number of coil turns will vary based on a variety of factors including pole pitch, pole count, stator ID, stator length, and connection (4Y vs. 8D), among others. For a motor this size, we require about 200 turns per phase and will fine tune these details as the design progresses.

Another factor that we will utilize here is configuration of coil turns and stator electrical connection. If we find that our required voltage is too high, we have a few remedies:

- If delta connected, decrease the number of turns and re-design the slots
- If wye connected and the ratio of required voltage to design voltage is  $\sim 170\%$ , connect in delta.
- If coil strip thickness is too thick to bend properly, consider doubling the number of turns per coil and halving the stator parallel branches (if possible).
- If there seems to be too much insulation cross section to copper cross-section in the slot, consider halving the number of turns per coil and double the stator parallel connections if possible).

There are other adjustments that may be made to the stator design to fine tune the coil geometry, voltage, and thermal loss.

### *Aluminum or Copper Rotor Conductors*

While aluminum is not as conductive as copper ( $\sim 45\%$ ), it is very light ( $\sim 2700 \text{ kg/m}^3$  for AL vs  $8900 \text{ kg/m}^3$  for CU). Even by using twice the aluminum, the overall weight of the rotor and the associated inertia is much less; also, aluminum has historically been much less costly than copper and will likely remain as such. Also, copper has a maximum peripheral speed of 60 m/s before material creep begins to be a problem and acceptable aluminum peripheral speeds are as high as  $90 \text{ m/s}$ <sup>12</sup>. Aluminum must be welded while copper is typically brazed<sup>13</sup>. Since our rotor is of moderate size and low maximum speed, we will opt for copper rotor conductors to begin the design process.

Starting design dimensions:

*Stator OD: 1200mm*

*Stator ID: 900mm*

*Stator Length = Rotor Length: 1000mm*

*Air Gap: 1mm*

*Rotor OD: 898mm (Stator ID - 2 \* Air Gap)*

*Rotor ID = Shaft OD: 180mm*

*Design Speed: 200 RPM*

*Design Num Poles: 24*

*Design Phase: 3*

*Design Voltage: 4000V*

*Design Shaft Power: 4500HP*

*Design Torque: 118,000 lbf-ft*

*Num Stator Slots: 144*

*Num Rotor Slots: 108*

*Stator Slot Width:  $0.5 * (900\text{mm} * \pi / 144 \text{ slots}) = 9.8\text{mm}$*

*Stator Slot Depth: 75mm*

*Back Iron Depth:  $\sim 70\text{mm}$*

*Slot Wedge Thickness: 2.5mm*

*Wedge/Air Gap Standoff = 1mm*

*Winding Connection = 8Y*

*Turns-per-coil = 11*

*Coil Pitch = 5*

*Number of Strands = 1 (one-in-hand)*

*Wire Width =  $\sim 8.3\text{mm}$*

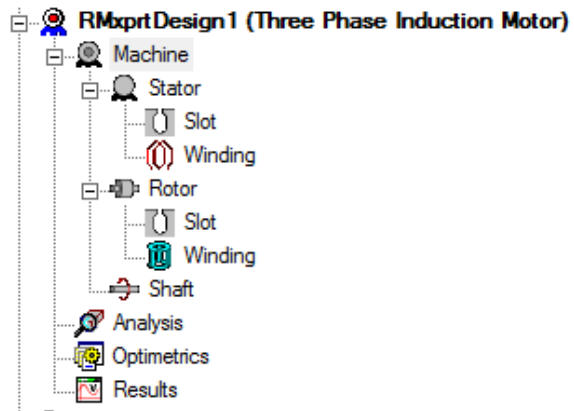
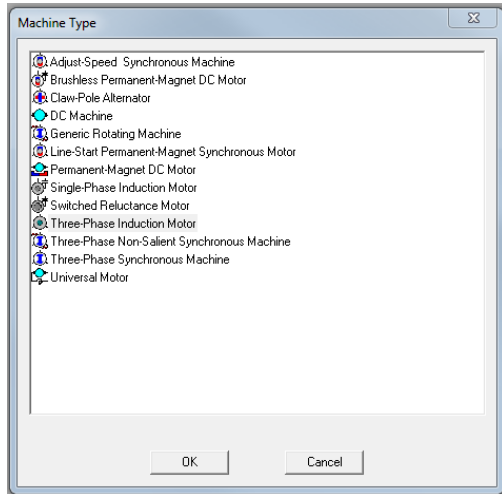
*Wire Thickness =  $\sim 2.5\text{mm}$*

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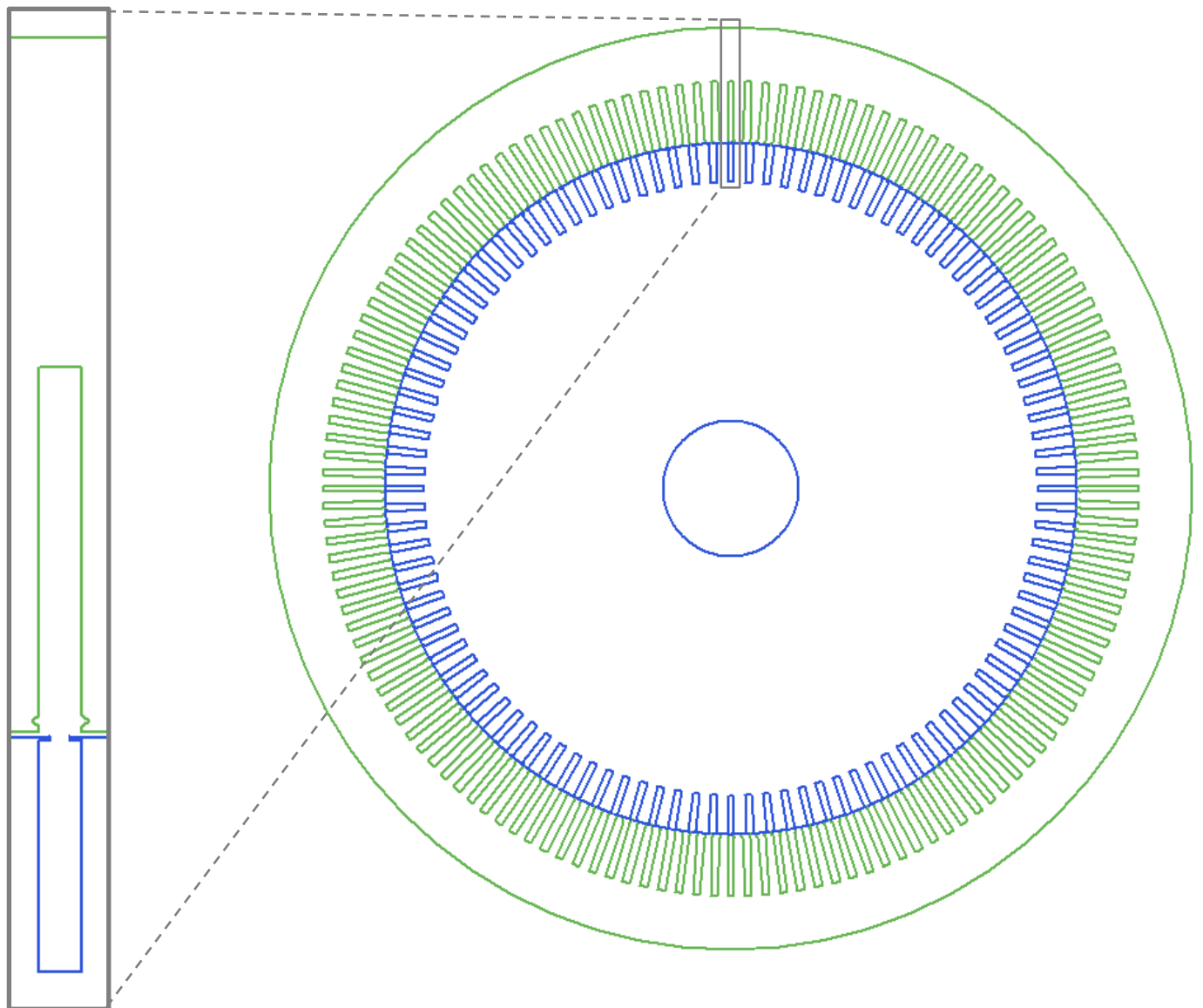
<sup>12</sup> Maximum peripheral speed is a function of the material creep stress limit. The applied stress is a function of the material density, location of the material relative to the axis of rotation, and rotational speed. The creep limit of Aluminum is lower than Copper but the density of Copper is so much higher that use of Aluminum becomes practical when high peripheral speeds are considered.

<sup>13</sup> For smaller rotors, aluminum die casting is very popular and quite cost effective. Copper die casting is developing as a technology but is much more costly than aluminum die casting due to tool wear, casting difficulties, and material costs.

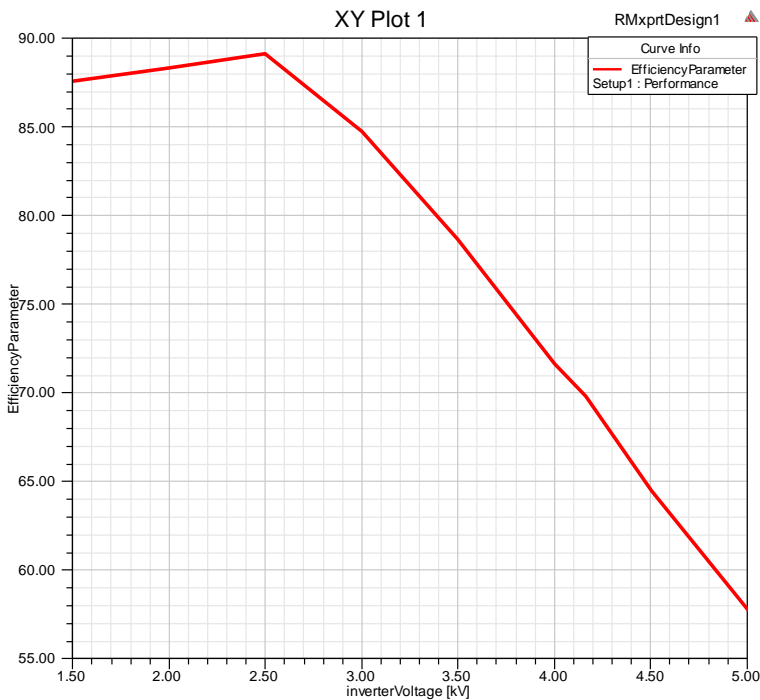
We begin our analysis by setting up the electrical machine design software. Once initialized, we enter our starting dimensions and perform a battery of simulations to assist in determining where to focus further optimization effort.



The resultant geometry appears as shown here (slot detail left, cross-section of motor on right):



The first analysis is initially disappointing resulting in a very poor efficiency (1.47 MW of loss!) Our power factor is also quite poor (0.156). We attack this issue by simply analyzing performance at several different input voltages in an effort to identify a trend.



$$N_{turns} = 11 * \sqrt{\frac{4000V}{2500V}} \approx 13.9 \text{ turns}$$

We re-simulate with 14 turns/coil and arrive at a more encouraging result but still not quite close enough. We still see that power factor is extremely low (0.240); understanding that higher pole count motors tend to have poor power factor; we focus our optimization efforts here. We opt to modify the winding/connection arrangement to an equivalent (10 turns/coil and 4Y connection) to provide more flexibility in coil design later.

A technique we can utilize to optimize the power factor is a plot of power factor vs. several independent variables; in the plots shown below, plotting efficiency and power factor together indicates that the highest power factor occurs at ~3500Vrms while the highest efficiency occurs at ~4500Vrms (see Figure 15). Adding another turn may help the power factor a bit but the gain would likely be small at this stage.<sup>14</sup>

A sweep of Stator ID reveals maximum efficiency and power factor at ~950mm instead of the original guess of 900mm (see Figure 15).

	Name	Value	Units
1	Stator Ohmic Loss	1332960	W
2	Rotor Ohmic Loss	83015.4	W
3	Iron-Core Loss	26211.1	W
4	Frictional and Windage Loss	288.276	W
5	Stray Loss	30213	W
6	Total Loss	1472690	W
7	Output Power	4566.8	HP
8	Input Power	4879560	W
9	Efficiency	69.8193	%
10	Power Factor	0.156154	
11	Rated Torque	166629	NewtonMeter
12	Rated Speed	195.243	rpm
13	Rated Slip	0.0237855	

As expected when we plot applied voltage vs. efficiency, we notice that maximum efficiency occurs at 2500V, not the designed 4000V. Motor voltage is directly proportional to motor inductance at a given frequency so we need 4000V/2500V = 160% of the inductance we currently have. Inductance is related to the square of the coil turns so we find that we need:

	Name	Value	Units
1	Stator Ohmic Loss	476730	W
2	Rotor Ohmic Loss	98072.7	W
3	Iron-Core Loss	22134.8	W
4	Frictional and Windage Loss	286.047	W
5	Stray Loss	30213	W
6	Total Loss	627436	W
7	Output Power	3356770	W
8	Input Power	3984210	W
9	Efficiency	84.2519	%
10	Power Factor	0.240185	
11	Rated Torque	164956	NewtonMeter
12	Rated Speed	194.323	rpm
13	Rated Slip	0.0283846	

<sup>14</sup> Indeed, a quick simulation shows that shifting to 11 turns-per-coil in 4Y connection results in a power factor of 0.543 @ 4000V while 10 turns per coil has a power factor of 0.537 @ 4000V – a marginal improvement in power factor.

Sweeping rotor bar geometry reveals that a power factor of 0.65 is only achieved with 8mm wide and 10mm wide rotor bars (Figure 17)...and then only when the bar depth is 30mm or less. Examination of a similar family of curves for efficiency (Figure 17) shows that maximum efficiency is achieved when using a 10-12mm bar 35-40mm deep. As a compromise, a 12mm x 35mm bar is selected for further analysis and optimization.

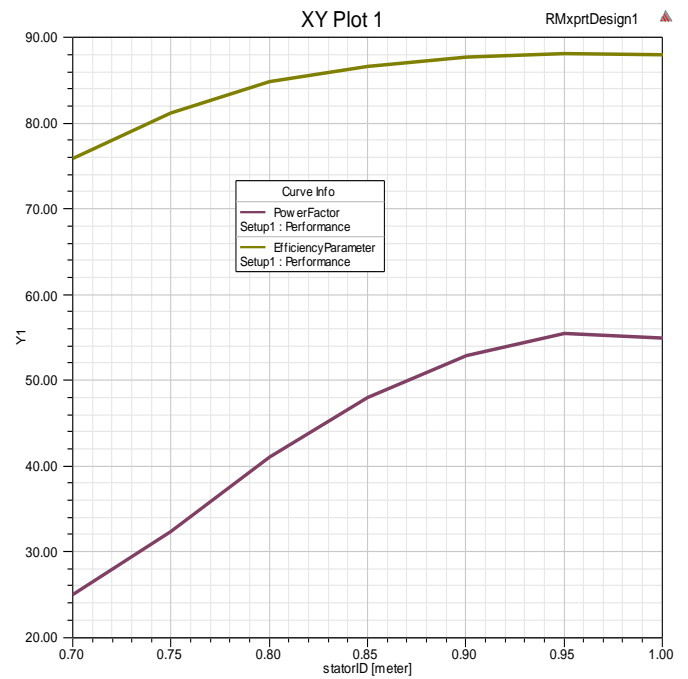
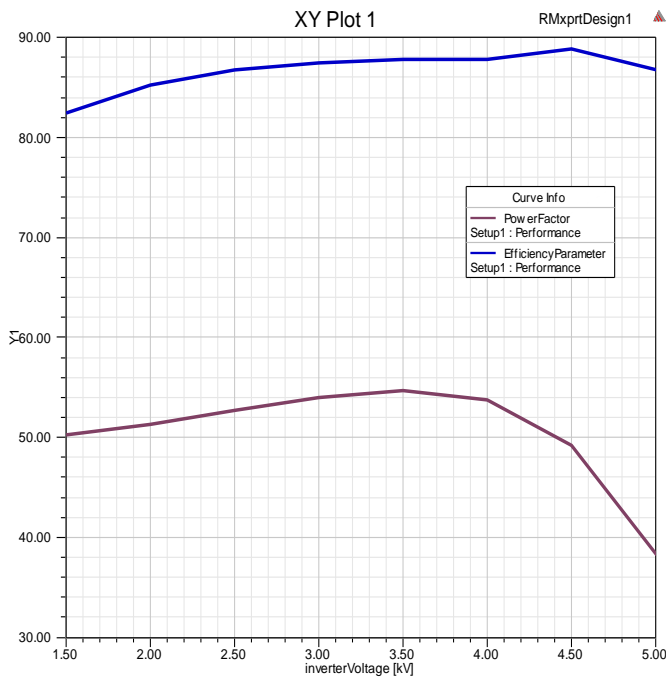


Figure 15 – Power Factor and Efficiency vs Inverter Voltage (Left) and Stator ID (Right)

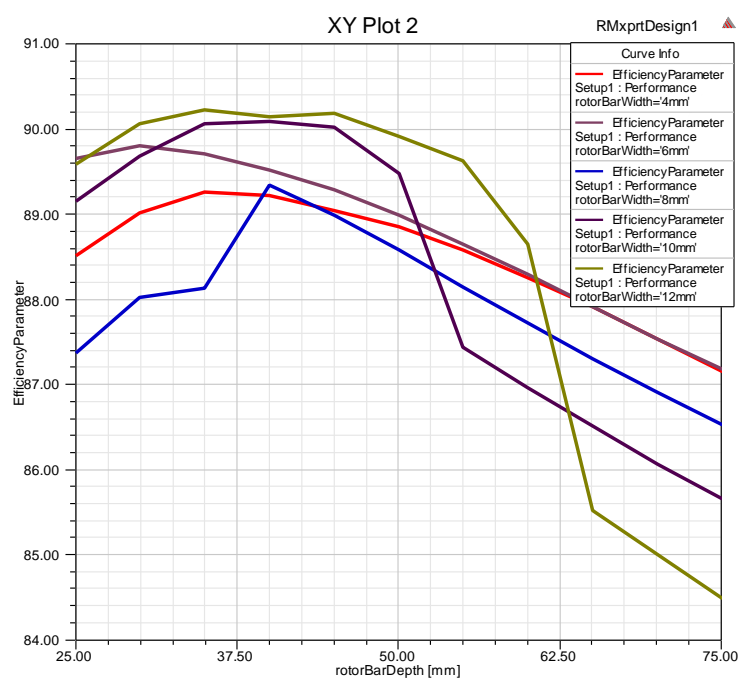
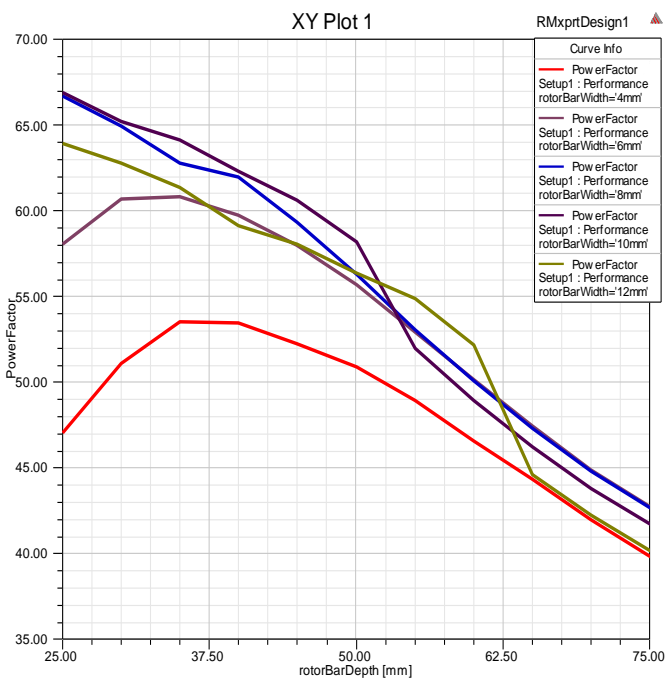


Figure 17 – Power Factor vs Rotor Bar Depth as Bar Width is Varied

Figure 17 - Efficiency vs Rotor Bar Depth as Bar Width is Varied

After applying the newly optimized geometry settings and running another base operating point simulation, we gather the performance data shown to the right. With only a few iterations and optimization sweeps, we have nearly achieved the design goals with only efficiency and power factor remaining outside of the acceptable range. Full load current is stated at 839A which is still well above the 744A target; keeping the current rating down as low as possible will be critical in keeping the size, weight, and cost of the drive as low as possible.

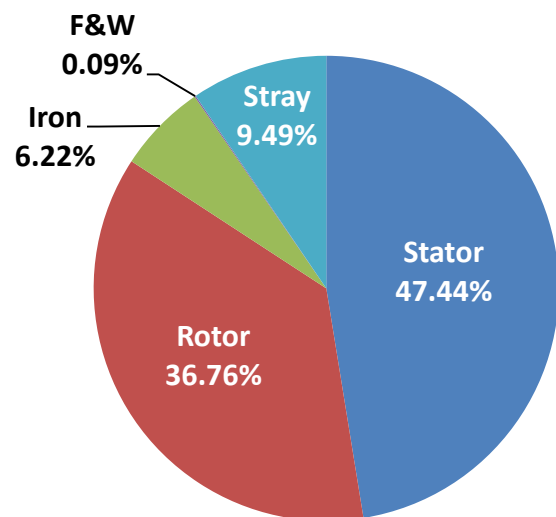
After refining the design<sup>15</sup>; similar sweeps were conducted to optimize the thickness of the back-iron while all other dimensions are held constant. Both the power factor and efficiency plots reached maximums at 30mm of back-iron depth resulting in 91.33% efficiency and 0.667 power factor.

	Name	Value	Units
1	Stator Ohmic Loss	184846	W
2	Rotor Ohmic Loss	132912	W
3	Iron-Core Loss	17782.7	W
4	Frictional and Windage Loss	281.49	W
5	Stray Loss	30213	W
6	Total Loss	366035	W
7	Output Power	3376510	W
8	Input Power	3742550	W
9	Efficiency	90.2196	%
10	Power Factor	0.613408	
11	Rated Torque	167562	NewtonMeter
12	Rated Speed	192.426	rpm
13	Rated Slip	0.0378698	

	Name	Value	Units
1	Stator Ohmic Loss	150951	W
2	Rotor Ohmic Loss	117326	W
3	Iron-Core Loss	19821	W
4	Frictional and Windage Loss	283.453	W
5	Stray Loss	30213	W
6	Total Loss	318595	W
7	Output Power	3356700	W
8	Input Power	3675300	W
9	Efficiency	91.3314	%
10	Power Factor	0.666702	
11	Rated Torque	165872	NewtonMeter
12	Rated Speed	193.246	rpm
13	Rated Slip	0.0337697	

This most recent design adjustment has increased the power factor to a level that satisfies the design goal; however, efficiency still suffers. By examining the performance parameters for this most recent simulation...taking note of thermal losses:

- Stator Ohmic Loss = 151kW
- Rotor Ohmic Loss = 117kW
- Iron-Core Loss = 19.8kW
- Friction/Windage Loss = 283W
- Stray Loss = 30.2kW



As shown in the pie chart to the right, the stator joule losses dominate followed closely by the rotor losses. Iron losses represent about 6% of the total losses in the machine. Stray losses are very difficult to address analytically as they account for induced currents in frame parts, shaft currents, rotor inter-bar currents, and other energy lost that is overly difficult to model accurately; for a machine this size, stray losses are assumed to be 0.9% of total shaft power in accordance with NEMA, IEC, and IEEE recommendations until detailed loss segregation testing can be done on a physical prototype. It is clear that effort is best spent optimizing on all ohmic losses in the machine as small efforts here are likely to produce the significant results.

The rotor conductor bars have already been optimized for efficiency and power factor so the only free geometries remaining on the rotor are the end ring dimensions. Thus far, the rotor end-ring cross-section has been fixed at 625mm<sup>2</sup> (25mm x 25mm). Simulation reports that rotor bar current density is 9.50 A/mm<sup>2</sup> while the rotor end-ring current density is reported as 9.33 A/mm<sup>2</sup>; increasing the rotor end-ring cross-section will reduce losses but at a diminishing

<sup>15</sup> Particularly in the stator slot region by properly defining actual insulation thickness and fully parameterizing the stator slot design

rate<sup>16</sup>. A quick sweep of the rotor end-ring confirms this suspicion as a doubling of the cross-section only increases efficiency from 91.33% to 91.50% (which represents a reduction of about 4kW in total heat).

Since the *stator* ohmic losses represent such a large proportion of the overall thermal loss, design modifications to the stator should have a much more profound impact on the critical output parameters. Generally speaking, increasing the dimensions of the stator conductors will:

- Consume a larger mass of copper; thereby increasing machine weight marginally<sup>17</sup> and cost appreciably.
- Reduce stator thermal losses in approximate proportion to the change in copper cross-section; thereby improving efficiency.
- Increases in coil volume will invariably displace steel from the stator laminations; reductions in ‘critical’ steel will tend to degrade power factor

The parameter sweeps shown at the right reveal a rather interesting trade-off and presents an excellent opportunity to ‘fine-tune’ the parameters. We observe that in general, increasing wire width or wire thickness tends to degrade power factor and simultaneously improves efficiency. The vigilant designer will select a coil wire strip width and thickness that provides the best trade-off between power factor degradation and improvements in efficiency.

We notice that on the efficiency plot (Figure 18 bottom), the 3mm and 2.5mm wire thicknesses tend to converge with wire widths more than about 8mm; the efficiency of the 2mm wire is not quite converged, but is ‘nearby’. We also notice that efficiency suffers significantly when considering 1mm thick wire; as a result, 1mm thick wire is removed from consideration.

By examining the power factor plot (Figure 18 top), we observe that the 3mm wire creates inferior power factors (<0.65) for all wire widths and so is removed from consideration.

When considering the 1.5mm, 2mm, and 2.5mm wire, the power factor tends to degrade more rapidly at wire widths in excess of 8mm. Conversely, the efficiency tends to plateau for the same wire sizes when wire width is higher than about 7mm. The following table (Table 1) summarizes possible combinations of wire dimensions and the resultant impact on power factor and efficiency.

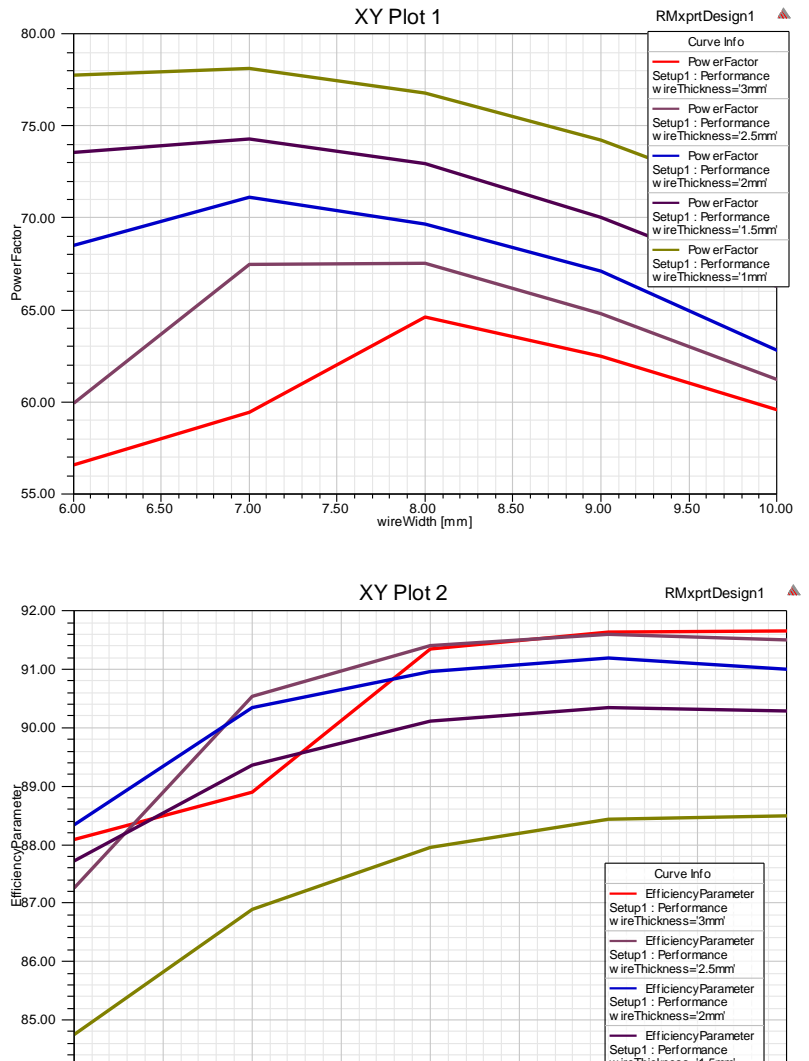


Figure 18 - Power Factor and Efficiency vs. Coil Conductor Geometry

<sup>16</sup> The improvements diminish since, as the rotor end ring resistance decreases, the rotor bars begin dominate the contribution to the total rotor impedance.

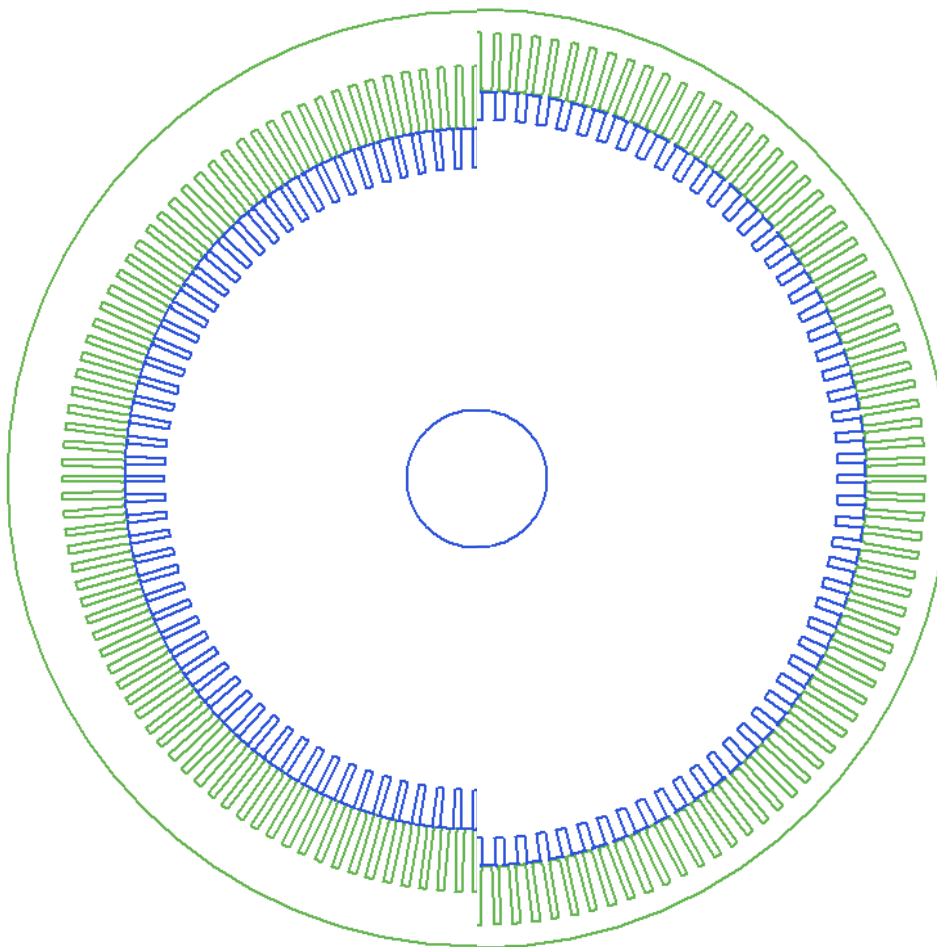
<sup>17</sup> As the coil dimensions increase, the slot dimensions must also increase; the net effect being a substitution of steel volume for copper volume. Copper, having a slightly higher density than steel, will increase machine weight consistent with this difference.

Table 1 - Comparison of Efficiency and Power Factor vs. Wire Dimensions

Width	Thickness			Width	Thickness		
	1.5	2.0	2.5		1.5	2.0	2.5
7.0	89.35%	90.33%	90.54%	7.0	0.742	0.711	0.675
7.5	89.73%	90.64%	90.96%	7.5	0.736	0.704	0.675
8.0	90.10%	90.95%	91.40%	8.0	0.729	0.697	0.675

The two tables (colored by value, green is preferred) clearly show the trade-offs. All power factors are higher than the design target of 0.65 so by this logic, the 8mm x 2.5mm wire is the optimum choice. If impact of cabling, switchgear, and drive is taken into account, the reduced current offered by the higher power factor of the 2mm wire may be attractive. If focused completely on efficiency, any of the lower right four wire combinations could be considered. 2mm x 7.5mm compared to the 2mm x 8mm wire suffers a significant efficiency penalty with only a minor improvement in power factor. When comparing 2mm x 8mm to 2.5mm x 7.5mm, the 2.5mm provides comparable efficiency with a moderate reduction in power factor so 2mm x 8mm is preferred here.

The 2.5mm x 8mm wire provides a significant increase in efficiency for a tolerable decrease in power factor with an associated 25% increase in coil copper consumption over the 2mm x 8mm wire while drive current is 749A vs 729A. With the reduced current demand of the 2mm x 8mm wire coupled with the reduced cost and tolerable efficiency penalty, we select this wire for our application. However, if during thermal simulation, the reduced efficiency of the 2.0mm wire proves overwhelming for the cooling system to maintain temperature, the 2.5mm wire may become a necessity.



*Re-Evaluate Design against Goals*

With several iterations of optimization complete, we can now re-examine the entirety of performance goals against the target specifications.

One can see by inspection of the comparison at the left the significant change in geometry due to optimization. Initial assumptions regarding back-iron depth and Stator ID are quite different even though the slot geometry changed very little while the Stator OD and Rotor ID didn't change at all.

Performance criteria at the base operating point:

<b>Criteria</b>	<b>24-Pole Design</b>	<b>Target/Limit</b>
Base Power	3.36 MW (4500 HP)	-
Base Speed	193.9 RPM	200 RPM
Base Torque	165,309 N-m (121,930 lbf-ft)	118,170 lbf-ft
Base Frequency	40 Hz	-
Base Voltage	4160 Vrms	-
Base Current	734 Arms	< 715A
Net Core Weight	8,284 kg (18,263 lb)	< 20,000 lbs
Efficiency	90.88%	> 93%
Rejected Heat	337 kW	253 kW
Power Factor	0.692	> 0.7

The table above summarizes the current status of the design; since Base Power, Base Frequency, and Base Voltage were inputs into the simulation, comparisons are omitted. The Base Speed is only slightly less than the design shaft speed of 200RPM (due to slip) – this is easily adjusted by the VFD by increasing output frequency to approximately 41.3 Hz. While improvements in efficiency and power factor were significant, the current requirement is over the target of 715 Arms and the thermal losses are 92 kW (33%) more than originally budgeted. Further optimizations may result in better performance criteria or other adjustments can be made to improve efficiency while degrading power factor (as shown previously). It may also be attractive to re-examine some of the early assumptions (i.e. number of slots, stator OD, etc) in an effort to explore improved design topologies.

The following table summarizes the results from a 12-Pole design optimization so that both 12-Pole and 24-Pole designs could be compared.

Table 2 - Comparison of 12-Pole and 24-Pole Designs

<b>Criteria</b>	<b>12-Pole Design</b>	<b>24-Pole Design</b>	<b>Target/Limit</b>
Base Power	3.36 MW (4500 HP)	3.36 MW (4500 HP)	-
Base Speed	194.5 RPM	193.9 RPM	200 RPM
Base Torque	164,811 N-m (121,560 lbf-ft)	165,309 N-m (121,930 lbf-ft)	118,170 lbf-ft
Base Frequency	20 Hz	40 Hz	-
Base Voltage	4160 Vrms	4160 Vrms	-
Base Current	<b>632 Arms</b>	<b>734 Arms</b>	< 715A
Net Core Weight	8,308 kg (18,316 lb)	8,284 kg (18,263 lb)	< 20,000 lbs
Efficiency	90.90%	90.88%	> 93%
Rejected Heat	336 kW	337 kW	253 kW
Power Factor	<b>0.804</b>	<b>0.692</b>	> 0.7

Table 2 briefly outlines and highlights the performance differences between the 12-Pole design and 24-Pole design motors. Both motors are designed to operate with the same input voltage and provide the same output torque at approximately the same speeds; weight and efficiency are nearly identical between the two machines. One major advantage one might quickly notice is the difference in full load current between the two machines. Higher pole machines of a given size class often suffer from inferior power factors – in some fixed frequency applications, the advantage of a lower shaft speed is worth the extra current capacity needed. For this example, the 12-Pole design enables the use of 14% smaller upstream drives, switchgear, transformers, and cabling than does the 24-Pole design with the only significant difference being the Base Frequency of 20Hz instead of 40Hz. It would be critical to the application to ensure that the drive control algorithms will remain sufficiently stable across 0-20Hz and that the bridge will have sufficient frequency resolution to control shaft speed, but the 12-Pole design would be the most probable selection.



## Next Steps

Further optimization of the high-level (bulk) parameter design may allow for further improvements in size, weight, or efficiency. Advanced numerical techniques could also be employed at this time in an effort to find a unique solution to the parameterized design that improves on one or more of the design criteria – genetic algorithms (GA's), Non-Linear Programming (NLP), and Pattern Searches may each result in superior parameter combinations that may have been missed or over-looked during simple one or two variable sweeps. Once a collection of similar designs have been compiled, scripting can be employed to automatically generate operating envelope speed-torque-power curves and efficiency maps that can be used to gain better insight into fitness for the application and potentially identify any design weaknesses<sup>18</sup>. Also at this stage of development, a formal design and specifications review should be conducted to ensure that integrated systems interfaces and inter-dependencies are properly addressed and identified.

Table 3 - 12-Pole, 4500 HP, 4 kV Induction Motor; Efficiency Map

100%	78.8	87.7	90.2	91.6	92.0	92.1	91.9	91.8	91.4	90.9
90%	77.4	86.8	89.5	90.9	91.6	91.8	91.4	91.2	90.5	90.0
80%	77.0	85.7	89.2	90.3	90.8	90.9	90.7	90.2	89.6	89.0
70%	75.1	84.4	88.1	89.3	89.9	90.1	89.6	89.3	88.6	87.6
60%	72.7	82.7	86.9	88.5	89.1	88.8	88.4	88.0	86.9	85.7
50%	69.6	81.3	86.0	86.9	87.5	87.4	86.9	85.9	84.6	82.9
40%	65.4	79.1	83.5	85.4	85.8	85.7	84.4	83.0	80.8	78.2
30%	59.8	76.0	81.1	83.4	83.2	82.0	80.0	77.2	73.4	65.6
20%	54.6	71.4	78.2	79.3	77.5	74.0	68.3	69.1	68.8	68.6
10%	47.4	67.2	70.0	62.4	45.4	45.2	45.0	44.8	44.6	44.4
	10%	20%	30%	40%	50%	60%	70%	80%	90%	100%

The efficiency map of Table 3 shows the efficiency trend at various speeds and power levels. Recall from Figure 12 that the power required will approximate a cubic function; cursory examination of the efficiency map shows that there is a significant improvement to be implemented during continued optimization to maximize efficiency in the power and speed ranges of interest (maximum efficiency is centered around 60% speed and 100% power...a region that is usually not reachable during normal vessel operation). Drive algorithm tuning may also provide some capability to adjust performance at various speeds and power levels but should only be relied upon for marginal adjustments.

After bulk design is 90% complete and summary performance is accepted, detailed Finite Element Analysis (FEA) on the electro-magnetic design and Computational Fluid Dynamics (CFD) for thermal design can begin. There is some benefit in performing magneto-static analysis but the majority of the effort will focus on transient analysis. It is during this stage that refinements will be made to the slot geometry and laminations to address flux concentrations, enhanced cooling strategies, and mechanical issues (strength, vibration, mounting, etc). A cyclic, iterative process of transient FEA, CFD, solid modelling, and numerical modelling is required to finish optimization; the majority of the designer's time is usually spent during this phase of design.

<sup>18</sup> For example, we notice that the efficiency is worst at low speed/low power operation. This is of little consequence since it is unlikely that the vessel would be operating in this region for extended periods of time. Maximum weight should be given to total expected energy consumption over the life of the vessel (...it makes little sense to be most efficient at 100% power if the vessel will operate at 70% power for the majority of its expected life).

## Concluding Remarks

Implementation of integrated system design and analysis by component providers can provide systems integrators (and eventually end-users) with highly optimized, efficient systems that reduce capital costs and life-cycle costs. Most systems can be appropriately modeled numerically to incorporate cost functions and weighting factors for a wide variety of criteria. A highly optimized, component designed for single speed use will often be detrimental to a larger integrated system when operated away from that ideal operating point since system level assumptions used during design are no longer valid (and are often not provided by the manufacturer nor requested by the systems designer/integrator). Integrated system-level component design is an engineering philosophy that when applied effectively, can enhance key criteria for minimal investment (and in some cases, will cost less).

This paper briefly outlines the high level design and selection process for a 5000 HP induction motor for a fictitious marine propulsion application. By examining the propulsion system as an integrated system, we have shown how an astute designer can make significant system level design trade-offs that have meaningful impact on capital expense, maintenance requirements, supporting infrastructure, operation flexibility, design flexibility, and construction flexibility. While the focus of this paper was on a marine propulsion example, this philosophy can be expanded and extrapolated to any system where variable speed motor operation is required or might be desired.

The majority of motor designs are generic or 'general purpose'; the trend over the past decade has been to apply a variable frequency drive to a general purpose induction motor. Too often, the selected motor has not been optimized for use in the chosen integrated system nor has it been optimized for use with a variable frequency drive. This article has presented a straight-forward method using first principles techniques that shows how small, seemingly innocuous changes in materials or geometry can have significant impact on any of several important operating parameters that might only occur at a single speed or power level that is not normally considered or that is not listed on a summary label plate.

Through application of integrated systems analysis, numerical modelling, and collaborative effort among component providers and systems designers; lighter, smaller, lower cost, more efficient, and higher performing systems can be created. A critical element to this approach is to enforce an integrated systems methodology at component design stages by engaging component providers as early as possible in system (or vessel) design and embracing critical analysis techniques relating to system interaction and inter-operability throughout the design process.

## References

- A. NEMA MG-1
- B. IEEE 112-2004
- C. Alger Motor Book
- D. Handbook of Electric Motors
- E. The Induction Machine Handbook